

# Manufacturing Data Fusion

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# Outline

- Introduction
- Ensemble Modeling for Data Fusion in Manufacturing Scale-up
- Other Research
- Summary

# Biography

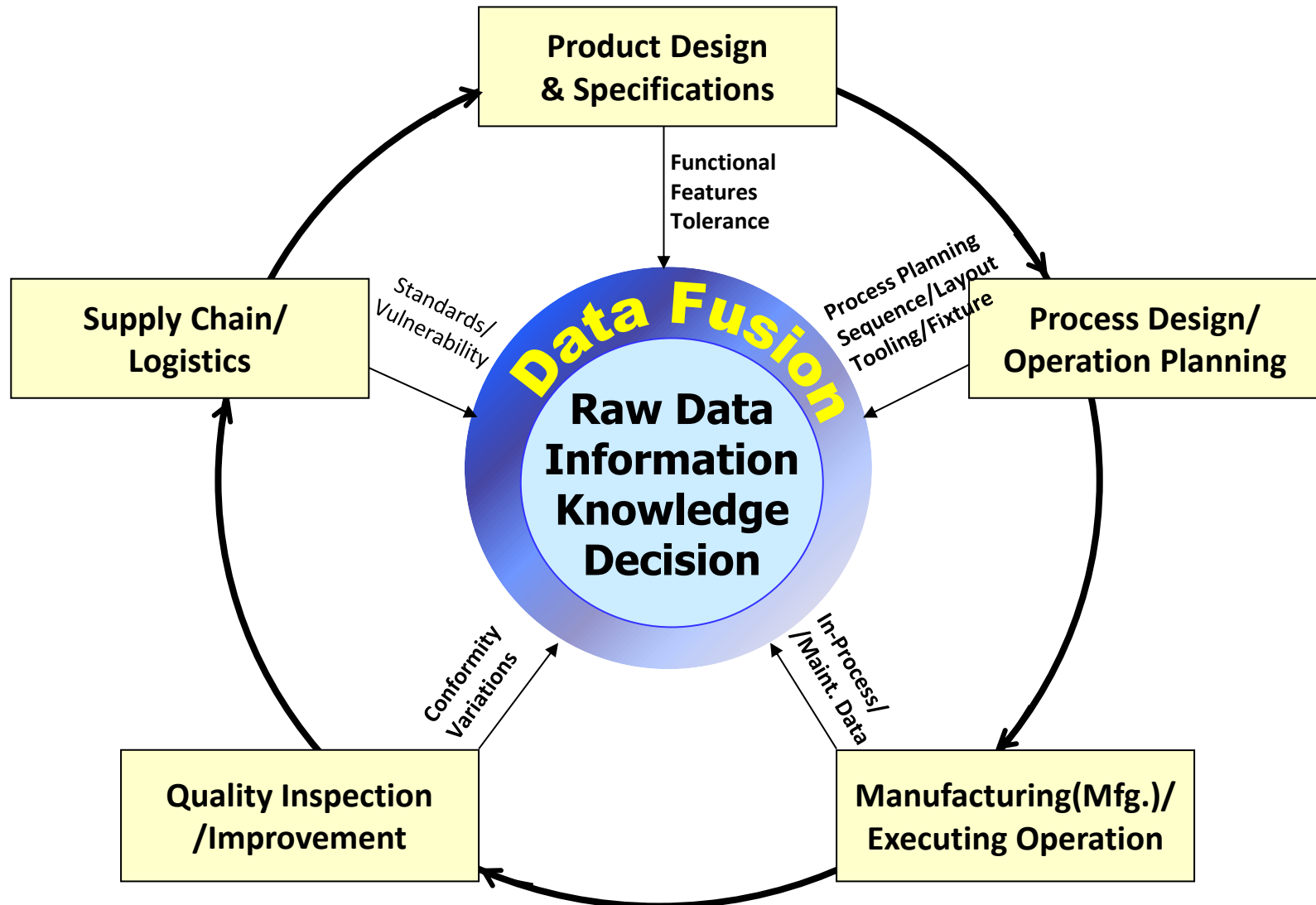
- **Education**

- B.Eng.: Electronic Engineering, Tsinghua Univ.
- M.S.: Industrial Engineering, Univ. of Michigan.
- M.A.: Statistics, Univ. of Michigan.
- Ph.D.: Industrial Engineering, Georgia Tech.

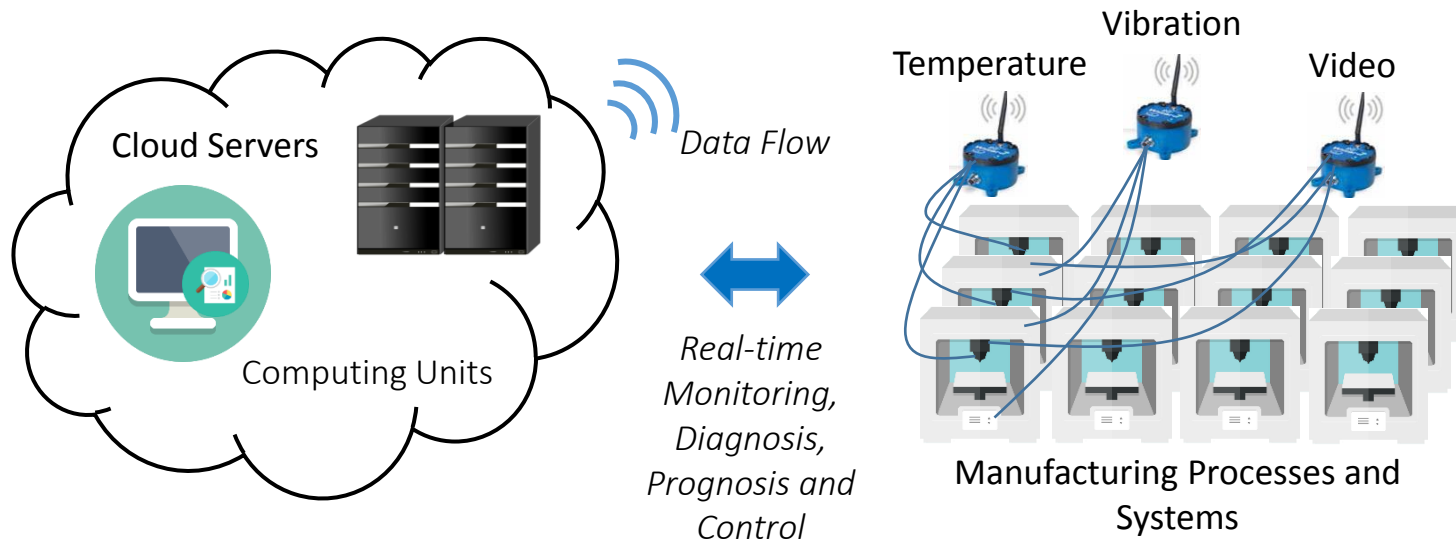
- **Research Interests**

- Data fusion in smart manufacturing
- Visualization of data with complex structures (manufacturing processes/systems, motion tracking data, enterprise profile)

# Data Fusion in Product Realization

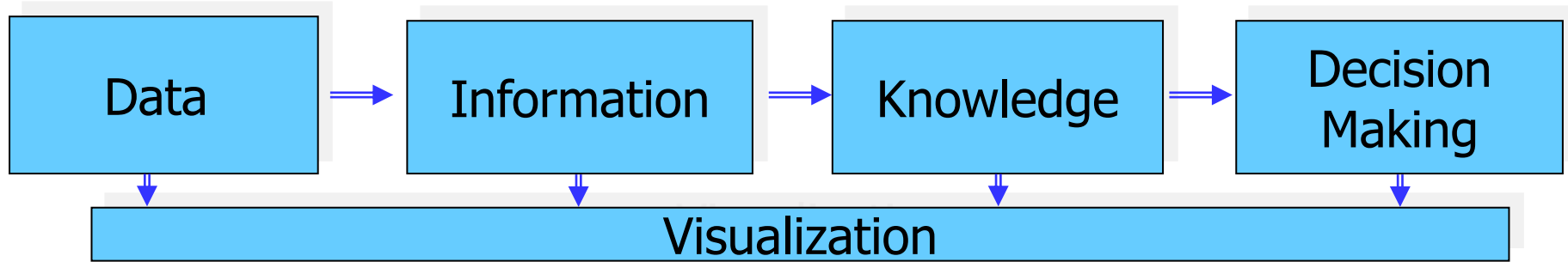


# Industrial Internet for Smart Manufacturing



Data-driven Modeling, Monitoring, Prognosis, Diagnosis,  
Control and Optimization

# Data Fusion in Smart Manufacturing

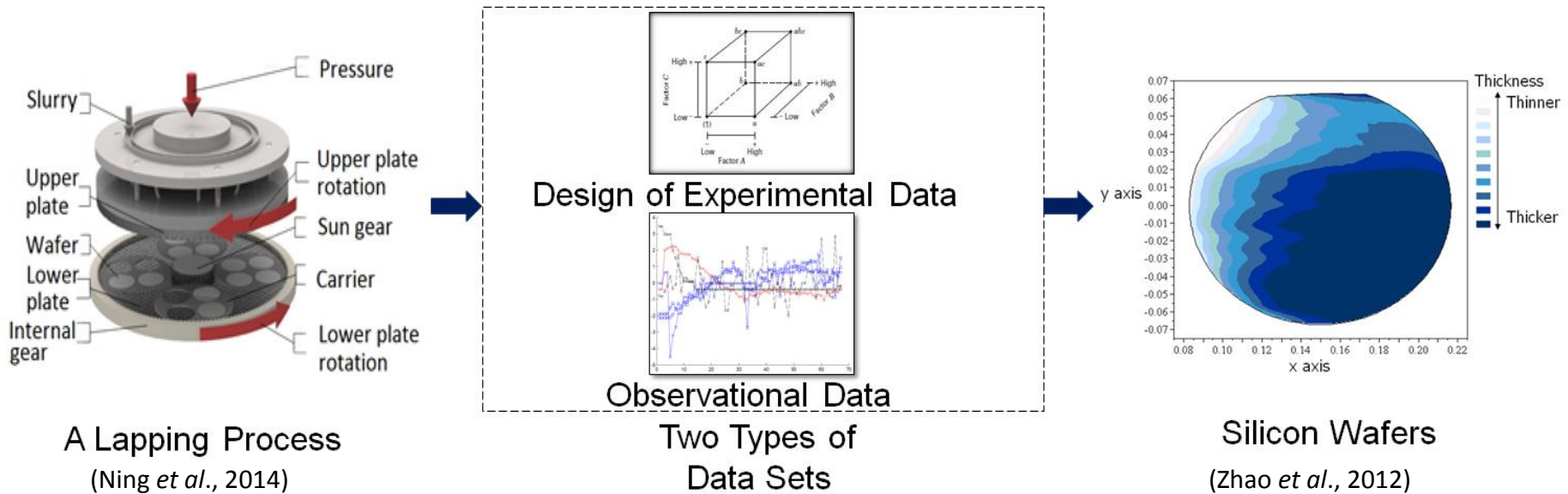


- Research Objective: Process data to support effective decision making in smart manufacturing (smart design, smart manufacturing operations, and smart services).
- Key Areas: Data Fusion Modeling, Process Monitoring, Control, 3D Cloud Data Analysis, Mfg. Visualization
- Key Industrial Applications: Additive Mfg. (Metal, Polymer, Electronics), Aero-engine Mfg., Baby Care Mfg., Continuous Fiber Mfg., Machining, Steel Mfg., Wafer Mfg.,etc.

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- **Ensemble Modeling for Data Fusion in Manufacturing Scale-up**  
*Joint work with Dr. Xinwei Deng @ VT Statistics*
- Other Research
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# Quality Control in Manufacturing Scale-up



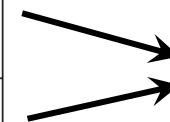
- Objective: to model the quality variables in scale-up manufacturing
- **Time consuming and difficult:**
  - Impact of noise factors (e.g., uncertainties from equipment)
  - Multiple rounds of modeling and process optimization (trial-and-error, or robust parameter design)
  - Model consistency based on the two types of data



# Complimentary Features of Data Sets

- **Design of Experiments (DOE)** is usually performed
  - to identify important process variables,
  - to control the noise factors, and
  - to determine initial recipes.
- **Validation production** is usually carried out after DOE
  - to obtain observational data, and
  - to validate the initial manufacturing recipe.
- Modeling and optimization performance is usually affected by sample size, data uncertainty, and range of predictors.

Data Type	Sample Size	Uncertainty	Range
Experimental	Small	Low	Large
Observational	Large	High	Small



***Complimentary  
Features →  
Data Fusion?***

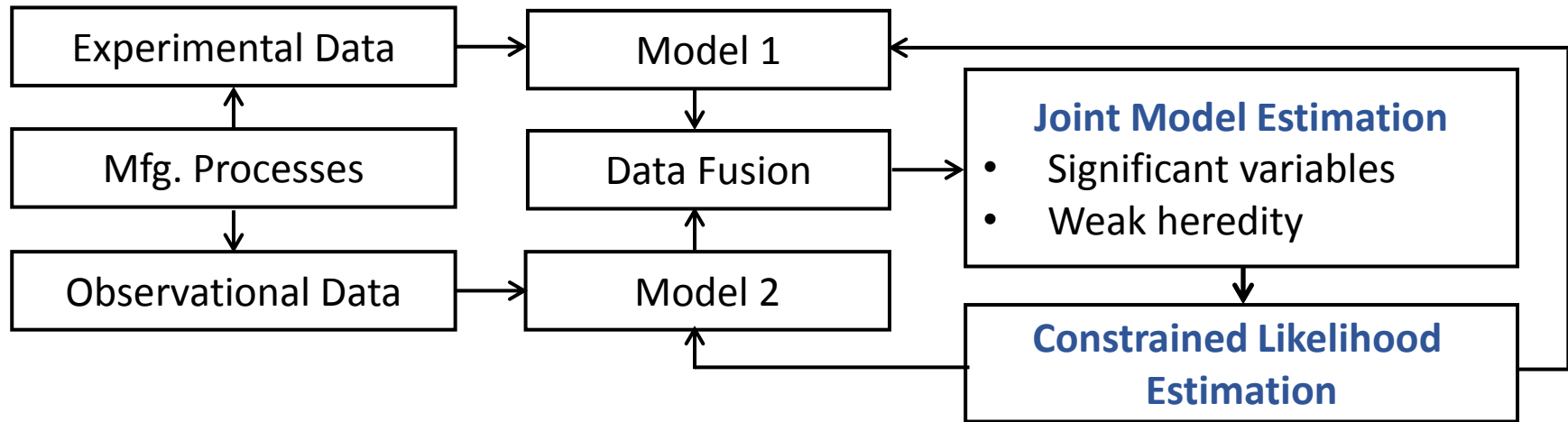
# Methods based Experimental Data

- Robust Parameter Design (RPD) (Taguchi, 1962; Wu and Hamada, 2000; Montgomery, 2005)
- RPD based feedforward/feedback control  
(Joseph, 2003; Dasgupta and Wu, 2006)
- DOE-based APC (Jin and Ding, 2004; Zhong *et al.*, 2010)
- Applications in discrete part mfg, nano material fabrications, etc. (Basumallick *et al.*, 2003; Dasgupta *et al.*, 2008...)
- **Limitations:** expensive for a large number of runs

# Methods based Observational Data

- Regression-based variation analysis (Fong and Lawless, 1998)
- Stream-of-Variation theory (Shi, 2006; Apley and Shi, 1998; Jin and Shi, 1999; Ceglarek and Shi, 1999; Huang *et al.*, 2003; Zhou *et al.*, 2003; Ding *et al.*, 2005; Liu *et al.*, 2010)
- Causation based variation reduction (Li and Shi, 2007; Li *et al.*, 2008)
- Regression tree based methods (Jin and Shi, 2012)
- **Limitations:** not applicable for unstable testing production  
model consistency issue

# Proposed Method



- Data fusion of experimental and observational data
- Two models: Model 1 for DOE and Model 2 for the mfg. system
- Assumptions:
  - (i) Two types of data with the same predictors and responses
  - (ii) Static process in one model iteration
  - (iii) Significant variables identified from the DOE model → significant in the final model

# Model Parameterization

- Denote the experimental (DOE) data as  $(z_i^{(1)}, y_i^{(1)}), i = 1, \dots, n_1$ , and observational (OBS) data as  $(z_j^{(2)}, y_j^{(2)}), j = 1, \dots, n_2$ . Here  $z^{(1)} = (x_1^{(1)}, \dots, x_p^{(1)})'$  and  $z^{(2)} = (x_1^{(2)}, \dots, x_p^{(2)})'$  contain the same  $p$  factors,  $y^{(k)}, k = 1, 2$  is univariate response, and  $\mathbf{x} = (x_1, \dots, x_p, x_1x_2, \dots, x_{p-1}x_p)'$

$$\text{Model 1} \longleftarrow y^{(1)} = \mathbf{x}^{(1)'} \boldsymbol{\beta}^{(1)} + \epsilon^{(1)}, \epsilon^{(1)} \sim N(0, \sigma_1^2),$$

$$\text{Model 2} \longleftarrow y^{(2)} = \mathbf{x}^{(2)'} \boldsymbol{\beta}^{(2)} + \epsilon^{(2)}, \epsilon^{(2)} \sim N(0, \sigma_2^2),$$

- Model parametrization through nonnegative garrote (Breiman,1995; Yuan and Lin, 2007)**

We re-parameterize the regression coefficients by

$$\beta_k = \theta_k \beta_k^{(ls)}, \beta_{kl} = \theta_{kl} \beta_{kl}^{(ls)}.$$

where  $\beta_k^{(ls)}$  and  $\beta_{kl}^{(ls)}$  are the least squared estimates, and  $\theta_k \geq 0$ ,  $\theta_{kl} \geq 0$  are the shrinkage coefficients, which can be estimated from data.

# Joint Variable Selection

- By defining  $\tilde{x} = Bx$ , where  $B = \text{diag}(\beta_1^{(ls)}, \dots, \beta_p^{(ls)}, \beta_{12}^{(ls)}, \dots, \beta_{p-1,p}^{(ls)})$  previous model can be converted as

$$\text{Model 1} \longleftarrow y^{(1)} = \tilde{x}^{(1)'} \theta^{(1)} + \epsilon^{(1)}, \quad \epsilon^{(1)} \sim N(0, \sigma_1^2),$$

$$\text{Model 2} \longleftarrow y^{(2)} = \tilde{x}^{(2)'} \theta^{(2)} + \epsilon^{(2)}, \quad \epsilon^{(2)} \sim N(0, \sigma_2^2),$$

- Such parameterization provides us the flexibility to impose various constraints for estimating parameters.
- Joint model estimation and variable selection by enforcing constraints**
  - Significant variables from DOE

$$\theta_k^{(1)} \leq \theta_k^{(2)}, \quad \forall k = 1, \dots, p, \quad \theta_{kl}^{(1)} \leq \theta_{kl}^{(2)} \quad \forall k \neq l.$$

- Weak heredity

$$\theta_{kl} \leq \max\{\theta_k, \theta_l\} \quad \longrightarrow \quad \theta_{kl} \leq \theta_k + \theta_l.$$

# Constrained Likelihood Estimation

$$\min \left\{ n_1 \left[ \log \sigma_1^2 + \frac{1}{n_1} \sum_{i=1}^{n_1} \frac{(y_i^{(1)} - \tilde{\mathbf{x}}_i^{(1)'} \boldsymbol{\theta}^{(1)})^2}{\sigma_1^2} \right] + n_2 \left[ \log \sigma_2^2 + \frac{1}{n_2} \sum_{j=1}^{n_2} \frac{(y_j^{(2)} - \tilde{\mathbf{x}}_j^{(2)'} \boldsymbol{\theta}^{(2)})^2}{\sigma_2^2} \right] \right\}$$

$$s.t. \quad \sum_{k=1}^p \theta_k^{(1)} + \sum_{k=1}^p \theta_k^{(2)} \leq M,$$

→ Theta constraints,  
 $M \geq 0$  : a tuning parameter

$$\theta_k^{(1)} \geq 0, \forall k, \quad \theta_k^{(2)} \geq 0, \forall k,$$

→ Definition

$$\theta_k^{(1)} \leq \theta_k^{(2)}, \quad k = 1, \dots, p,$$

$$\theta_{kl}^{(1)} \leq \theta_{kl}^{(2)} \quad \forall k \neq l, k, l = 1, \dots, p,$$

} Significance from DOE

$$\theta_{kl}^{(1)} \leq \theta_k^{(1)} + \theta_l^{(1)}, \quad \forall k \neq l, k, l = 1, \dots, p,$$

$$\theta_{kl}^{(2)} \leq \theta_k^{(2)} + \theta_l^{(2)}, \quad \forall k \neq l, k, l = 1, \dots, p,$$

} Weak Heredity

- This optimization is solved by an iterative algorithm.
- The tuning parameter is selected using BIC.

# Simulation Study

## Simulation Setup

	Factors	Interaction	Heredity	Sigma	Sample Size	Range
<b>Exp. 1</b>	5(4)	10(8)	Weak	2 (1/5/10)	24 (1/3/5)	[-1, 1] (1, 0.5, 0.3)
<b>Exp. 2</b>	10(7)	45(15)	Strong	2 (1/5/10)	64 (1/3/5)	[-1, 1] (1, 0.5, 0.3)
<b>Exp. 3</b>	10(7)	45(15)	Weak	2 (1/5/10)	64 (1/3/5)	[-1, 1] (1, 0.5, 0.3)

*Example 3:*  $y = 1.60x_1 + 4.01x_2 + 3.51x_3 + 2.36x_4 + 1.40x_7$   
 $+ 1.93x_8 + 2.48x_9 + 4.66x_1x_2 + 3.78x_1x_3$   
 $+ 2.34x_1x_4 + 3.33x_1x_7 + 4.85x_1x_8 + 2.87x_1x_9$   
 $+ 1.45x_2x_3 + 3.40x_2x_4 + 3.34x_2x_7 + 5.20x_2x_8$   
 $+ 1.89x_2x_9 + 2.33x_3x_4 + 1.97x_7x_8 + 4.91x_8x_9$   
 $+ 2.44x_8x_{10} + \epsilon.$

We fit the model based on a training set, and predict on a test set (uniformly over the input variable space).



# Simulation Results- Example 3

The average of MSPE based on 50 simulation replicates  
in Example 3 (weak heredity)

		$R_{OBS}/R_{DOE} = 1$			$R_{OBS}/R_{DOE} = 0.5$			$R_{OBS}/R_{DOE} = 0.3$		
$n_2/n_1$	Method	$\frac{\sigma_2}{\sigma_1} = 1$	$\frac{\sigma_2}{\sigma_1} = 5$	$\frac{\sigma_2}{\sigma_1} = 10$	$\frac{\sigma_2}{\sigma_1} = 1$	$\frac{\sigma_2}{\sigma_1} = 5$	$\frac{\sigma_2}{\sigma_1} = 10$	$\frac{\sigma_2}{\sigma_1} = 1$	$\frac{\sigma_2}{\sigma_1} = 5$	$\frac{\sigma_2}{\sigma_1} = 10$
1	$BM_{DOE}$	11.96 (0.93)	11.99 (0.61)	10.58 (0.54)	11.95 (0.60)	11.82 (0.70)	11.49 (0.63)	10.62 (0.53)	11.40 (0.66)	12.49 (0.73)
	$BM_{OBS}$	19.54 (1.02)	66.92 (5.00)	142.64 (11.88)	72.10 (5.60)	316.06 (21.37)	541.61 (39.24)	Accurate Prediction over the Range		
	$BM_{CBD}$	2.81 (0.09)	7.09 (0.35)	12.23 (0.79)	Robust Model Structure					
	$EM$	3.50 (0.10)	6.24 (0.25)	8.36 (0.43)						
3	$BM_{DOE}$	11.37 (0.68)	10.83 (0.55)	12.99 (0.58)	11.38 (0.63)	11.63 (0.67)	11.46 (0.61)	12.01 (0.61)	12.05 (0.59)	12.42 (0.72)
	$BM_{OBS}$	4.39 (0.11)	10.90 (0.58)	18.47 (1.38)	10.78 (0.59)	38.23 (3.59)	72.78 (6.65)	27.26 (1.81)	73.52 (8.64)	189.51 (18.98)
	$BM_{CBD}$	1.97 (0.07)	5.25 (0.23)	8.33 (0.42)	3.49 (0.21)	5.51 (0.31)	6.45 (0.17)	4.97 (0.29)	5.03 (0.05)	5.97 (0.08)
	$EM$	2.56 (0.06)	4.05 (0.13)	5.09 (0.09)	3.65 (0.12)	4.27 (0.06)	4.85 (0.15)	4.69 (0.13)	4.52 (0.05)	4.82 (0.08)
5	$BM_{DOE}$	12.69 (0.90)	11.25 (0.68)	13.06 (0.76)	12.59 (0.75)	10.67 (0.49)	11.55 (0.72)	11.63 (0.57)	11.98 (0.64)	11.73 (0.63)
	$BM_{OBS}$	3.48 (0.07)	8.41 (0.36)	14.56 (1.06)	Accurate Prediction with Limited Samples			13.48 (1.13)	60.87 (6.41)	100.21 (12.34)
	$BM_{CBD}$	1.62 (0.06)	4.98 (0.16)	8.97 (0.40)				3.97 (0.28)	5.09 (0.09)	6.85 (0.11)
	$EM$	2.02 (0.07)	4.16 (0.07)	5.99 (0.20)				3.39 (0.06)	4.44 (0.07)	4.93 (0.08)

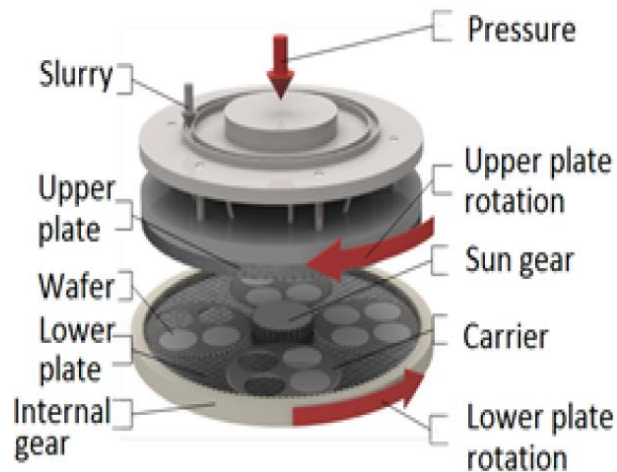
# Simulation Results- Variable Selection

# of False Selection for Example 3,  
average of 50 simulation replicates

$n_2/n_1$	Method	$R_{OBS}/R_{DOE} = 1$			$R_{OBS}/R_{DOE} = 0.5$			$R_{OBS}/R_{DOE} = 0.3$		
		$\frac{\sigma_2}{\sigma_1} = 1$	$\frac{\sigma_2}{\sigma_1} = 5$	$\frac{\sigma_2}{\sigma_1} = 10$	$\frac{\sigma_2}{\sigma_1} = 1$	$\frac{\sigma_2}{\sigma_1} = 5$	$\frac{\sigma_2}{\sigma_1} = 10$	$\frac{\sigma_2}{\sigma_1} = 1$	$\frac{\sigma_2}{\sigma_1} = 5$	$\frac{\sigma_2}{\sigma_1} = 10$
1	$BM_{DOE}$	22.68	23.00	20.32	22.84	22.64	22.22	21.24	20.40	23.04
	$BM_{OBS}$	26.90	26.76	27.86	27.26	28.88	26.90	27.28	27.12	27.18
	$BM_{CBD}$	5.78	13.00	19.68	8.06	14.78	20.16	9.42	13.56	21.32
	EM	11.24	13.76	16.08	13.76	14.88	14.76	14.68	15.84	14.96
3	$BM_{DOE}$	21.86	21.74	24.18	20.72	22.24	21.60	22.24	23.02	22.30
	$BM_{OBS}$	13.30	21.74	22.18	17.62	22.46	22.28	20.74	22.12	22.62
	$BM_{CBD}$	4.76	15.42	21.08	6.08	16.08	20.24	8.20	17.34	20.98
	EM	7.90	13.24	13.12	8.36	13.78	13.26	11.68	14.64	12.04
5	$BM_{DOE}$	22.50	21.96	23.12	21.52	21.82	21.56	21.84	21.98	20.52
	$BM_{OBS}$	11.18	21.36	21.94	16.24	21.66	22.32	19.36	22.16	22.16
	$BM_{CBD}$	4.10	16.52	21.10	5.50	15.50	21.90	8.32	15.42	21.60
	EM	7.06	13.44	13.34	7.42	12.38	12.88	10.68	11.52	12.30

- Note that Examples 1-3 have 15, 55 and 55 predictors, respectively.
- The EM provides more accurate variable selection than the other approaches.

# Case Study



A diagram of the lapping process  
(Ning *et al.*, 2014)

## Data Format

Variable Type	Variable Name	Physical Meaning
Controllable Process Variable	Pressure ( $N/m^2$ )	The high pressure of the upper to lower plate
	Rotation (Rpm)	The rotation speed
	LowPTime (Sec.)	The time for low pressure
	HighPTime (Sec.)	The time for high pressure
Covariate	CTHK0 ( $\mu m$ )	Central thickness of wafers
	TTV0 ( $\mu m$ )	Total thickness variation of wafers
	TIR0 ( $\mu m$ )	Total indicator reading of wafers
	STIR0 ( $\mu m$ )	Site total indicator reading of wafers
	BOW0 ( $\mu m$ )	Deviation of local warp at the center of wafers
	WARP0 ( $\mu m$ )	Maximum of local warp of wafers
Quality Response	CTHK1 ( $\mu m$ )	Central thickness of wafers after lapping

# Case Results - Prediction

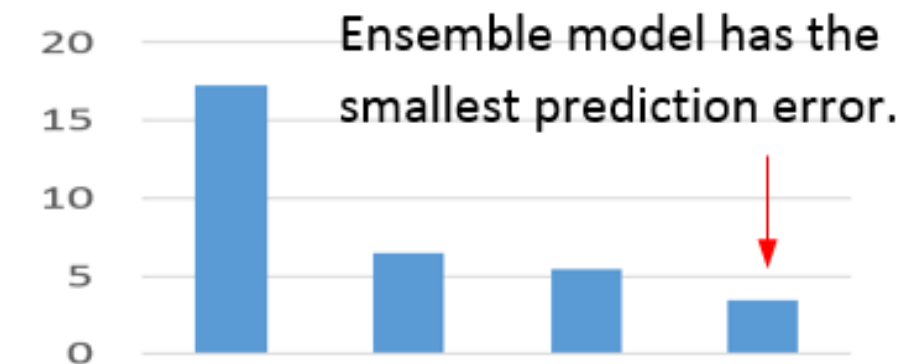
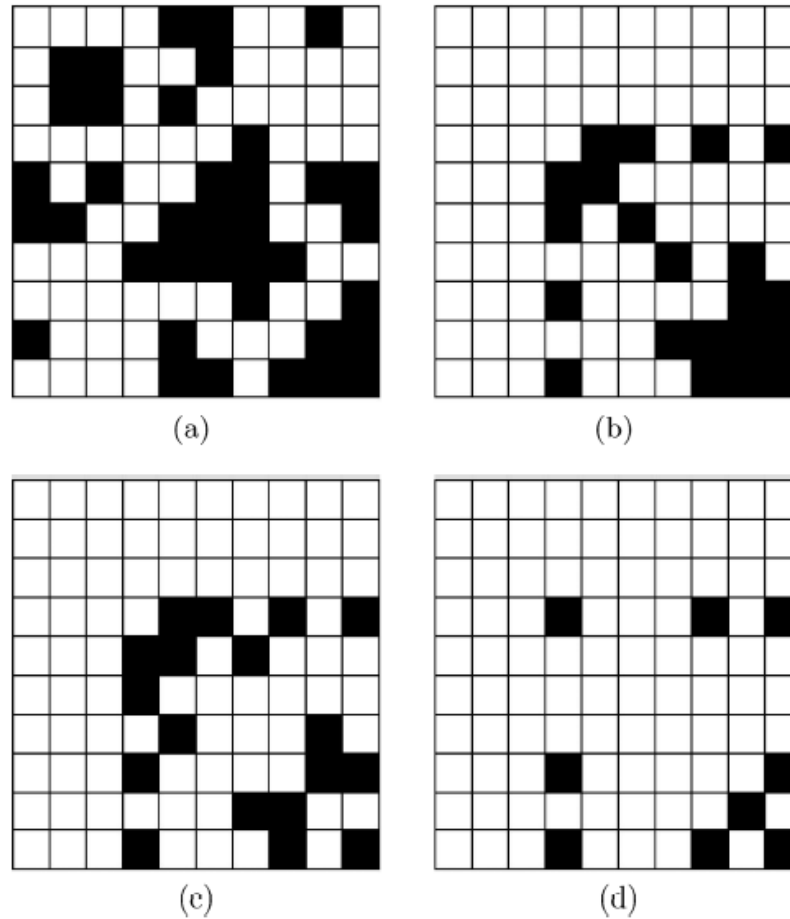


Figure. Prediction errors of models in a lapping process (left to right: model based on DOE data, OBS data, combined DOE and OBS data. ensemble model)

# Case Results - Variable Selection



**Fig. 2.** Variable selection on the wafer data for (a)  $BM_{DOE}$ ; (b)  $BM_{OBS}$ ; (c)  $BM_{CBD}$ ; and (d)  $EM$ . The order of predictors are Pressure, Rotation, LowPTime, HighPTime, CTHK0, TTV0, TIR0, STIR0, BOW0, and WARP0.

# Summary of Ensemble Modeling

- Manufacturing Scale-up is an important step in product realization. However, the process modeling and recipe optimization involves multiple iterations of experiments and testing runs.
- Both experimental and observational data are collected in the scale-up efforts, while current methodologies focus on the modeling and improvement based on single type of data.
- We propose **an ensemble modeling strategy for data fusion** of the two types of data for manufacturing process modeling by
  - Model parametrization through nonnegative garrote
  - Joint variable selection in two models with DOE and heredity constraints
  - Constrained likelihood estimation
- Future work:
  - Bayesian framework for data fusion and other variable selection
  - Joint design of experiments and data selection
  - Modeling between different generations of equipment

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# Modeling Methodologies for Better Quality and Higher Efficiency (Modeling, Monitoring and Control)



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# Summary

- Data fusion is about the integration of different types of variables, data sets and information!
- The visualization is about delivery the *right information* to the *right person* at the *right time*!
- Examples are shown in many different applications.

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Thank you!  
Questions?